LIMIT STATE AND PROBABILISTIC FORMATS IN THE ANALYSIS OF BRACING PIERS OF ANNULAR CROSS-SECTIONS

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Abstract. The expediency and efficiency of concrete bridge piers of annular cross-sections reinforced by steel bars uniformly distributed throughout their perimeter are considered. Modelling of permanent and live load effects and bearing capacity of bracing tubular piers is presented. The features of unsophisticated probability-based design formats are analysed. A simplified but fairly exact analysis of eccentrically loaded piers by limit state and probabilistic approaches is provided. The design practice of bracing tubular piers using limit state and probabilistic approaches is illustrated by a numerical example.

Keywords: bridge piers, tubular structures, road traffic loads, eccentric loading, limit state design, probability-based design.

1. Introduction

Any bridge system and its components must be economically reasonable, structurally appropriate and aesthetically satisfactory. The concrete piers of annular cross-sections satisfy these requirements and provide the most appropriate moments of inertia of cross-sections in two main directions. Bracing piers of bridges are fixed at their base and top in order to provide the load from decks to foundations. Therefore, they can transmit to the foundations all effects caused by vertical and horizontal random forces and are assumed to contribute to the overall horizontal stability of a bridge.

The reliability verification and rationality assessment of structures may be made by using partial safety factors (in Europe) and load and resistance factors (in the USA and other countries) based on probability criteria or by applying probability-based approaches. The choice of the level of reliability of structural members and their systems should take into account the predicted consequences of failure in terms of risk in life and potential economic losses. However, the reliability level of columns designed by semi-probabilistic methods may be differ considerably (Diniz 2005). On the other hand, reliability verification formats based on probabilistic concepts help us evaluate objectively all uncertainties of design models and ascertain effective solutions of structures.

The results of this study involve the formulations of limit state and safety margin criteria, as well as the perfections of load effects, bearing capacity and survival probability formats for piers of annular cross-sections reinforced by steel bars uniformly distributed throughout their perimeters. They encourage designers and highway engineers to use the presented unsophisticated semi-probabilistic and probabilistic approaches in design practice of tubular piers of bridges.

2. Compressive forces and bending moments

The permanent gravity forces of piers \( N_G = N_{G1} + N_{G2} \) are caused by self-weight of structures, \( G_1 \), and roadway surfacing weight, \( G_2 \). The value \( N_{G1} \) also depends on propped and unpropped members of continuous beams (Kudzys et al. 2007). The coefficients of variation of these loads are \( \delta G_1 = 0.10 \) and \( \delta G_2 = 0.25 \) (Czarnecki, Nowak 2008; Eamon, Nowak 2004). The surfacing weight, \( G_2 \), may be determined taking into account possible additional roadway topping.

For the general verifications of bridge piers, the transient live load models must cover most of the traffic effects. The representing variable live gravity and horizontal longitudinal forces \( N_Q \) and \( Q_l \) are caused by heavily-loaded trucks, cars and special vehicles. The horizontal force \( Q_l \) consists of braking, temperature and wind components spreading out over the entire pier cap.
For the 75-year of girder bridges service, the coefficient of variation of static live loads, $\delta Q_{sl}$, can vary from 0.14 to 0.18 (Czarnecki, Nowak 2008; Eamon, Nowak 2004; Szerszen et al. 2005). For two heavily loaded trucks travelling side-by-side, the mean value of a dynamic load factor $Q_{d}/Q_{ia}$ may be taken as 0.10 with the coefficient of variation of $Q_{d}/Q_{ia} = 0.80$ (Eamon, Nowak 2004). Thus, the coefficient of variation of bridge live loads may be expressed as:

$$
\delta Q = \left[ \frac{\delta^2 Q_{sl}}{Q_{sl}} + \left( \frac{Q_{d}/Q_{ia}}{Q_{ia}} \right)^2 \right]^{\frac{1}{2}} + 2\delta Q_{sl} \times \frac{Q_{d}/Q_{ia}}{Q_{ia}} \delta Q_{d}/Q_{ia}.
$$

(1)

It is equal to 0.22–0.26 and may be taken as $\delta Q = 0.25$.

Low bracing piers ($h < 15$ m) may be considered as eccentrically loaded columns. According to EN 1992-2:2005 Eurocode 2: Design of Concrete Structures – Concrete Bridges – Design and Detailing Rules, the first order eccentricity of force $N$ of bracing piers (Fig. 1a) may be given by:

$$
e = e_o + e_{Ql} + e_{NG} + e_{NQ} =
\frac{Q_{d}h_3}{3EI} + \frac{N\varepsilon h^2}{2EI}.
$$

(4)

Its mean and variance are as follows:

$$
e_m = e_o + \frac{Q_{d}h_3}{3EI_{m}} + \frac{N\varepsilon h^2}{2EI_{m}} (N_{Gm} + N_{Qm});
$$

(5)

$$
\sigma^2 e = \sigma^2 e_{Ql} + \sigma^2 e_{NG} + \sigma^2 e_{NQ} +
2\left( \frac{\partial e}{\partial Q_l} \right)_m \left( \frac{\partial e}{\partial N_{Q}} \right)_m \sigma_{Ql} \sigma_{NQ} =
\left[ \frac{h^3}{3EI_{m}} \right]^2 \sigma^2 Q_l +
\left[ \frac{e_o h^3}{2EI_{m}} \right]^2 \left( \sigma^2 N_G + \sigma^2 N_Q \right) +
\left[ \frac{Q_{d}h^3}{3EI_{m}} \right]^2 + \left[ \frac{N\varepsilon h^2}{2EI_{m}} \right]^2 \times
\left( N_{Gm}^2 + N_{Qm}^2 \right) \sigma^2 (EI) +
2\left[ \frac{h}{3EI_{m}} \right] \times \frac{e_o h^2}{2EI_{m}} \sigma_{Ql} \sigma_{NQ}.
$$

(6)

where $K_c$ – the factor for effects of cracking, creep and sustained loads, where $\Phi = 1.2–2.0$ is the basic creep coefficient of concrete, whose value depends on its strength class, dimensions of cross-sections of piers and their environmental conditions; $M_{OG} = N_G e_o$ and $M_{OE} = Qh + N_G e_o$ – the 1st order bending moments caused by permanent and total load effects; $E_c$ – the modulus of elasticity of a concrete; $I = \frac{\pi r_4^4}{4} - r_1^4$ – the moment of inertia of a cross-section.

The 2nd order eccentricity of the applied compressive force $N_E = N_G + N_Q$ is defined as:

$$
e = e_o + e_{Ql} + e_{NG} + e_{NQ} = \frac{Q_{d}h_3}{3EI} + \frac{N\varepsilon h^2}{2EI}.
$$

(4)
From Eq (3), the mean and variance of a flexural stiffness of pier shafts may be expressed as:

\[
\begin{align*}
(El)_m &= K_{cm} E_{cm} l_{cm} = \\
&= \frac{0.3}{1 + 0.5 \Phi} \frac{M_{Gm}}{M_{cm}} E_{cm} l_{cm},
\end{align*}
\]

(7)

\[
\sigma^2(El) = (K_{cm} l_m)^2 \sigma^2 E_c + (K_{cm} E_{cm})^2 \sigma^2 l_m,
\]

(8)

where the variances of the modulus of elasticity \(E_c\) and the moment of inertia \(l_i\) of considered pier shafts are calculated using the coefficients of variation \(\delta E_c = 0.15\) (JCSS 2000) and \(\delta l = \delta A_e = \frac{1.2 - r_i}{150 (r_2 - r_i)} \geq 0.02\), where \(r_i = \frac{r_1 + r_2}{2}\).

The total destroying moment of bracing piers is expressed as:

\[
M_E = M_Q + M_G = Q h + N_G e + N_G e.
\]

(9)

The means and variances of its components are:

\[
M_{Qm} = Q_{im} h + N_{Qm} e_m,
\]

(10)

\[
\begin{align*}
\sigma^2 M_Q &= h^2 \sigma^2 Q_i + \sigma^2 N_Q^2 + 2h_m e_m \sigma Q_i \sigma N_Q, \\
M_{Gm} &= N_{Gm} e_m,
\end{align*}
\]

(11)

(12)

\[
\begin{align*}
\sigma^2 M_G &= e^2 \sigma^2 N_G + N_{Gm} \sigma^2 e.
\end{align*}
\]

(13)

When the design eccentricity \(e_d = e_y + e_{Old} + e_{Nlb}\) the design value, \(M_{Ed}\), of the total bending moment by (9) is equal to \(\gamma_f \gamma_E M_{Ed}\), where \(\gamma_f = 1.35\) (ENV 1991-3:1995, Eurocode 1 - Part 3, Basis of Design and Actions on Structures. Traffic Loads on Bridges) is the partial safety factor for actions and \(M_{GEd} = Q_{Ed} h + N_{QEd} e_d\) is its characteristic value.

3. Resisting moment

The modelling of stress-strain state and bearing capacity of eccentrically loaded concrete piers of annular cross-sections should take consideration their mechanical features. According to Вадлуга (1979, 1984), the ultimate bending moment \(M_R\) (Fig. 1b) of columns reinforced by hot-rolled steel bars could be expressed as:

\[
M_R = 1.2 r_i (A_{fs} f_{st} + N) \left\{ 1 - \frac{A_{fs} f_{st} + N}{A_{fs} f_{sc} + A_{fs} f_{sc}} \right\}.
\]

(14)

The characteristic values of reinforcement strength in tension, \(f_{stk}\), and compression, \(f_{scm}\), should not be more as \(f_{stk}\) and 500 MPa, respectively. The coefficients of variation of reinforcement strengths \(f_{stk}\) and \(f_{scm}\) in tension and compression zones of cross-sections may be calculated as \(\delta f_{stk} = (\delta f_{stk}^2 + \delta f_{scm}^2)^{1/2} = 0.10\), where the components \(\delta f_{stk} = 0.06\) (JCSS 2000) and \(\delta f_{scm} = 0.08\) (Вадлуга 1979) define their statistical deviations and the errors of right-angled epures of stresses.

According to JCSS (2000), Holicky and Markova (2007), the mean strength of hot rolled bars in tension and compression \(f_{stk} = f_{scm} = 560\) MPa. By Kudzys and Kliukas (2008), when high-strength coldworked steel is used, its conventional mean strength in tension and compression may be defined as \(f_{stk} = 500\) MPa and \(f_{scm} = 600\) MPa.

The compressive strength of concrete in tubular piers is presented as:

\[
f_{cc} = \alpha_{cc} k_3 f_{ck},
\]

(15)

where \(f_{ck}\) is its cylinder strength, MPa;

\[
\alpha_{cc} = 1 - 0.2 \frac{M_G}{M_E}
\]

(16)

and

\[
k_3 = 1 - 0.004 f_{ck} \leq 0.85
\]

(17)

are the factors of the sustained load and stress block, respectively. According to Kudzys and Kliukas (2008), the coefficient of variation of concrete strength is \(\delta f_{ck} = 0.089 + 3 \times (70 - f_{ck})^2 \times 10^{-5}\).

For design practice, Eq (14) may be rewritten in the form:

\[
M_R = \frac{T_1 T_3}{T_{lm}},
\]

(18)

where

\[
T_1 = A_{fs} f_{sc} + A_{fs} f_{ck},
\]

(19)

\[
T_2 = 1.2 r_i (A_{fs} f_{st} + N),
\]

(20)

\[
T_3 = A_{fs} f_{sc} + A_{fs} f_{ck} - N.
\]

(21)

The statistics of resistance \(R = M_R\) of pier shafts under bending with concentrical compressive force are given by:

\[
R_{lm} = \frac{T_{lm} T_{3m}}{T_{lm}},
\]

(22)

\[
\begin{align*}
\sigma^2 R &= \left[ \frac{T_{2m} (T_{lm} - T_{3m})}{T_{lm}^2} \right]^2 \times \\
&\left\{ A_{fs}^2 \sigma^2 f_{ck} + f_{ckm}^2 \sigma^2 A_{fs} + A_{fs}^2 \sigma^2 f_{sc} \right\} + \\
&\left[ \frac{T_3}{T_{lm}} (1.2 r_i T_{lm} - T_{3m}) \right]^2 \sigma^2 f_{st} + \\
&\left[ \frac{1.2 r_i T_{lm} - T_{3m}}{T_{lm}} \right]^2 \sigma^2 N,
\end{align*}
\]

(23)

where the variances of random variables are calculated by the expressions:

\[
\begin{align*}
\sigma^2 f_{cc} &= (\delta f_{cc}^2 + f_{ck})^2, \\
\sigma^2 A_{fs} &= (\delta A_{fs}^2 + A_{fs})^2, \\
\sigma^2 f_{sc} &= (\delta f_{scm}^2 + f_{scm})^2,
\end{align*}
\]
The statistics of random bending moments may have the forms:

\[
\begin{align*}
\sigma^2(\theta M_G) & = \theta^2 M_G \sigma^2 R + M^2_{Gm} \sigma^2 \theta M \sigma^2 \theta M, \\
\sigma^2(\theta M_Q) & = \theta^2 M_Q \sigma^2 Q + M^2_{Qm} \sigma^2 \theta M \sigma^2 \theta M.
\end{align*}
\]

where \( M^2_{Gm}, \sigma^2 R, M^2_{Qm}, \sigma^2 Q \) are calculated from Eqs (10)–(13).

For the sake of simplified but fairly exact probabilistic analysis of pier shafts, it is expedient to present Eq (24) in the form:

\[
Z = R_c - M_c,
\]

where

\[
\begin{align*}
R_c &= \theta R - \theta M M_G, \\
M_c &= \theta M M_Q(t)
\end{align*}
\]

are the conventional resistance and bending moment of pier shafts, respectively. Their statistics are defined as:

\[
\begin{align*}
R_{cm} &= (\theta R R)_m - (\theta M M_G)_m, \\
\sigma^2 R_c &= \theta^2 R \sigma^2 R + R^2 \sigma^2 \theta R^2 + \theta^2 M \sigma^2 M_G^2 + \\
& \quad M^2_{Gm} \sigma^2 \theta M^2, \\
M_{cm} &= (\theta M M_Q)_m = Q_{cm} h + N_{Qm} e_m, \\
\sigma^2 M_c &= h^2 \sigma^2 Q + N^2_{Qm} \sigma^2 e + e_m \sigma^2 N_Q + \\
& \quad 2 h e_m \sigma N Q\sigma Q + M^2_{Qm} \sigma^2 \theta M^2.
\end{align*}
\]

The parameters \( R_c \) and \( M_c \) are statistically independent variables. Therefore, the survival probability of piers may be calculated by the formula

\[
P_S = P\{R_c > M_c\} = \int_0^\infty f_R(x) F_M(x) dx,
\]

where \( f_R(x) \) is the density function of \( R_c \) by (32) and \( F_M \) – the cumulative distribution function of \( M_c \) by (33).

The survival probability of piers may be introduced by the reliability index

\[
\beta = \Phi^{-1}(P_S),
\]

where \( \Phi^{-1}(P_S) \) – the inverse of the standard normal distribution. For columns designed by limit state methods, this index is between 3.3 and 5.0. It increases significantly if a reinforcement ratio increases and a concrete compressive strength decreases (Diniz 2005).

According to EN 1990:2002 Eurocode: Basis of Structural Design, the target reliability index, \( \beta_T \), of structural
members may change from 3.3 to 4.3, depending on their failure consequence classes. For eccentrically loaded reinforced concrete columns and piers, the index $\beta_T$ must be not less 3.5 and may be selected equal to 4.0 because their failure can be more brittle comparing to a failure of bending members (Szerszen et al. 2005; Szerszen, Nowak 2003).

5. Numerical illustration

5.1. The parameters of analysis

The bracing piers (Fig. 2) of annular cross-sections of the cross-street bridge in Kaunas are subjected to permanent and variable vertical forces $N_G = N_{G1} + N_{G2}$ and $N_Q$, as well as horizontal braking force $Q_l$. Their characteristic values are presented as:

$$N_{Gk} = 2.45 + 0.84 = 3.29 \text{ MN},$$
$$N_{Qk} = 2.60 \text{ MN},$$
$$N_{Ek} = 3.29 + 2.60 = 5.89 \text{ MN},$$
$$Q_{lk} = 0.617 \text{ MN}.$$

According to Eq (2), the eccentricity $e_o = 0.063 \text{ m}$. The geometrical and mechanical parameters of piers are as follows:

$$h = 6.75 \text{ m},$$
$$r_2 = 0.75 \text{ m},$$
$$r_1 = 0.59 \text{ m},$$
$$r_s = 0.69 \text{ m},$$
$$A_c = 0.0225 \text{ m}^2 \left(28032 \text{ S500}\right),$$
$$A_{cm} = 0.652 \text{ m}^2,$$
$$\rho_m = \frac{A_c}{A_{cm}} = 0.0346,$$
$$I = \pi \left(\frac{r_2^4 - r_1^4}{4}\right) = 0.1533 \text{ m}^4,$$
$$\delta A_c = \delta I = \frac{1.2 - r_c}{150(r_2 - r_1)} = 0.022,$$
$$\sigma^2 A_c = 0.00021 \text{ m}^4,$$
$$\sigma^2 I = 0.0000114 \text{ m}^8.$$

According to Eurocode recommendations, the partial safety factors are:

$$\gamma_c = 1.5,$$
$$\gamma_s = 1.15,$$
$$\gamma_f = \gamma_G = \gamma_Q = 1.35.$$

The parameters of the concrete C35/45 are given by:

$$f_{ck} = 35 \text{ MPa},$$
$$f_{cm} = 43 \text{ MPa},$$
$$\alpha_{ccm} = 0.981,$$
$$k_3 = 0.85,$$
$$f_{ccm} = \alpha_{ccm} k_3 f_{cm} = 35.56 \text{ MPa},$$
$$\delta f_c = 0.125,$$
$$\sigma^2 f_c = (0.125 \times 35.56)^2 = 20.09 \text{ MPa}^2,$$
\(\alpha_{cd} = 1.0,\)
\[E_{cm} = 35 \text{ GPa},\]
\[\sigma^2E_c = (0.15 \times 35)^2 = 27.56 \text{ GPa}^2,\]
\[E_{cd} = 35/1.2 = 29.17 \text{ GPa.}\]

Thus, \(f_{cd} = k_f f_{ck} = 19.833 \text{ MPa}, \Phi = 1.9.\)

The parameters of reinforcing bars of the class S500 B are defined as:
\[f_{yk} = 500 \text{ MPa},\]
\[f_{std} = f_{scd} = f_{scm} = 560 \text{ MPa,}\]
\[f_{stm} = 560 \text{ MPa} \quad \text{(JCSS 2000; Holicky, Markova 2007)}, \]
\[\delta_f = 0.10, \quad \sigma^2f_{st} = (0.10 \times 560)^2 = 3136 \text{ (MPa)}^2,\]
\[E_s = 200 \text{ GPa}.\]

The statistics \(\theta_{Mm} = 1.0, \sigma\theta_M = 0.1, \theta_{Rm} = 1.02, \sigma\theta_R = 0.08.\)

5.2. Limit state analysis

The design value of flexural stiffness by (3) for pier shafts is defined as:
\[(EI)_d = \frac{0.3}{1 + 0.5 \times 1.9 \times 0.278} \times \frac{3.29 \times 0.0965}{1.286} \times 1286 \text{ MNm}^2.\]

Thus, according to Eq (4), the design eccentricity
\[e_d = e_o + e_{Qld} + e_{Nld} = 0.063 + 0.0664 + 0.0089 = 0.1383 \text{ m.}\]

The design values of the destroying forces and bending moments of considered piers are:
\[Q_{ld} = \gamma_f Q_{lk} = 0.833 \text{ MN},\]
\[N_{Ed} = \gamma_f(N_{Gk} + N_{Qk}) = 7.952 \text{ MN},\]
\[M_{Ed} = Q_{ld}e_d + N_{Ed}e_d = 0.833 \times 6.75 + 7.952 \times 0.1383 = 6.73 \text{ MNm.}\]

According to Eq (18), the design value of the resisting moment is expressed as:
\[M_{Rd} = \frac{T_{2d}T_{3d}}{T_{1d}} = \frac{14.70 \times 14.76}{32.50} = 6.67 \text{ MNm} = M_{Ed} \approx 6.73 \text{ MNm}.\]

Thus, the piers are suitable for the considered bridge.

5.3. Probability-based analysis

The mean values and variances of forces are as follows:
\[N_{Gm} = N_{Gk} = 3.29 \text{ MN};\]
\[\sigma^2N_G = (0.1 \times 3.29)^2 = 0.1084 \text{ (MN)}^2;\]
\[N_{Qm} = \frac{N_{Qk}}{1 + \beta_{0.98}^2\delta_{Q}} = 1.789 \text{ MN},\]
\[\sigma^2N_Q = (0.25 \times 1.789)^2 = 0.2 \text{ (MN)}^2;\]
\[N_{Em} = 3.29 + 1.789 = 5.079 \text{ MN},\]
\[\sigma^2N_E = 0.1084 + 0.2 = 0.3084 \text{ (MN)}^2;\]
\[Q_{lm} = \frac{Q_{lk}}{1 + \beta_{0.98}^2\delta_{Q}} = 0.424 \text{ MN},\]
\[\sigma^2Q_l = (0.25 \times 0.424)^2 = 0.01124 \text{ (MN)}^2.\]

The factor \(K_{cm} = \frac{0.3}{1 + 0.5 \times 1.9 \times 0.278} = 0.2826.\)

Therefore, the statistics of flexural stiffness of piers by (7) and (8) are:
\[(EI)_m = K_{cm}E_{cm}I_m = 0.2825 \times 35 000 \times 0.1533 = 1516 \text{ MNm}^2\]

and
\[\sigma^2(EI) = (K_{cm}E_{cm})^2\sigma^2f_c + (K_{cm}E_{cm})\sigma^2I = 52 800 \text{ (MNm)}^2.\]

From Eqs (5) and (6), the statistics of the second order eccentricity are:
\[e_m = 0.063 + 0.02867 + 0.00313 + 0.0017 = 0.0965 \text{ m,}\]
\[\sigma^2e = (0.703 + 0.003 + 0.0025 + 0.061) \times 10^{-4} = 0.000077 \text{ m}^2.\]

According to Eqs (25)–(28) and Eqs (36), (37), the statistics of bending moments are as follows:
\[(\theta_{Mm}) = M_{Gm} = N_{Gm}e_m = 3.29 \times 0.0965 = 0.318 \text{ MNm},\]
\[\sigma^2(\theta_{Mm}) = 3.29^2 \times 0.000077 + 0.0965^2 \times 0.1084 + 0.318^2 \times 0.01 = 0.00285 \text{ (MNm)}^2,\]
\[M_{cm} = (\theta_{Mm})m = 0.424 \times 6.75 + 1.789 \times 0.0965 = 3.034 \text{ MNm},\]
\[\sigma^2M_c = (\theta_{Mm})I_m = 6.75^2 \times 0.01124 + 1.789^2 \times 0.000077 + 0.0965^2 \times 0.2 + 0.0965 \times 0.447 \times 0.106 + 3.034^2 \times 0.01 = 0.668 \text{ (MNm)}^2.\]
According to Eqs (22), (29) and (30), the statistics of shaft resistance under bending with a concentrical force are:

\[ R_m = M_{Rm} = \frac{T_{2m} T_{3m}}{T_{1m}} = \frac{14.64 \times 30.86}{48.55} = 9.306 \text{ MNm} \]

\[ (\theta_R)_{m} = 1.02 \times 9.306 = 9.492 \text{ MNm} \]

\[ \sigma^2 R = 0.1253 + 0.1777 + 0.01408 = 0.3438 \text{ (MNm)}^2 \]

\[ \sigma^2 (\theta R) = 1.02^2 \times 0.3438 + 9.306^2 \times 0.0064 = 0.9119 \text{ (MN)}^2 \]

From Eqs (34) and (35), the statistics of conventional resistance are:

\[ R_{cm} = 1.02 \times 9.306 - 0.318 = 9.174 \text{ MNm} \]

\[ \sigma^2 R_{cm} = 0.9119 + 0.0029 = 0.9148 \text{ (MNm)}^2 \]

According to Eqs (38) and (39), the survival probability and reliability index of pier shafts are as follows:

\[ P_s = 0.999985 \] and \[ \beta = 3.93 \] and \[ \beta = 4.0 \]. Thus, their structural safety is sufficient and the constructive solution is effective.

The dimensions and the reinforcement of considered bracing pier satisfy reliability requirements of the current limit state and suggested probability-based design methods. The cross-sectional areas of concrete and reinforcing bars of solid and tubular pier shafts (Fig. 2) respectively are of the size: \[ A_c = 4.73 \text{ m}^2 \], \[ A_f = 0.0364 \text{ m}^2 \], and \[ 2A_{f1} = 1.304 \text{ m}^2 \]. However, the solid concrete pier is in need of a great amount of the transient reinforcement. There seems to be a clear rational use of concrete pier shafts of annular cross-sections.

6. Conclusions

The concrete bracing piers of annular cross-sections reinforced by steel bars uniformly distributed throughout their perimeter may be treated as economically reasonable and constructively appropriate structures for bridges. The analysis of bearing capacity and reliability of fairly complicated eccentrically loaded shafts of pier may be successfully based on the semi-probabilistic and full probabilistic concepts and approaches, presented in this paper. In both cases, the destroying and resisting bending moments of bracing piers are calculated in a single engineering manner by Eqs (9) and (14). The statistics of a shaft resistance may be expressed by Eqs (22) and (23).

For road bridges, the live load, \( Q \), can be described by a lognormal distribution with a coefficient of variation \( \delta Q = 0.25 \). The quantitative reliability index \( \beta \) by Eq (39) is indispensable in the objective assessment of a structural safety level of bridge pier and for an acceptability of their constructive solutions. The target reliability index \( \beta_T \) for pier shafts may be selected equal to 4.0. The presented design methods and their numerical illustration show that the prediction of a survival probability of piers, including their reliability index, may be based on unsophisticated probabilistic approaches. It may stimulate engineers, having a min of appropriate skills, to use full probabilistic approaches in design practice more courageously and effectively.

References


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